

Beam-beam compensation at the Tevatron

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FNAL

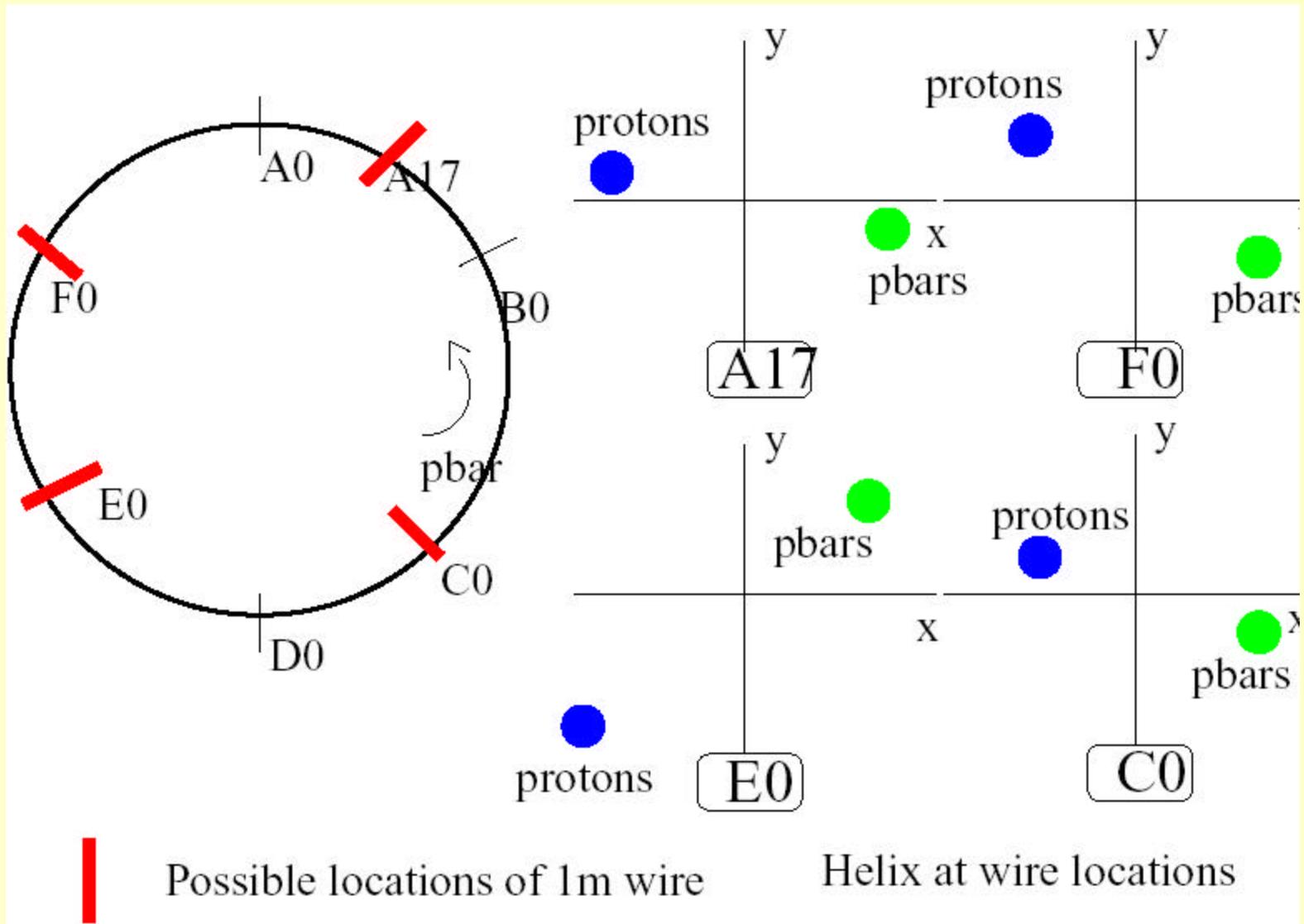
Why beam-beam compensation?

- At **injection energy** (150 GeV)
long-range forces cause pbar losses (5-15%)
- During **the ramp**
long-range forces cause pbar losses (5-15%)
- During **the low-beta squeeze**
long-range forces cause p and pbar losses (< 5%)
- During **collisions**
head-on and long-range forces cause emittance growth and occasionally large detector backgrounds (from protons) and lifetimes < 20hrs.

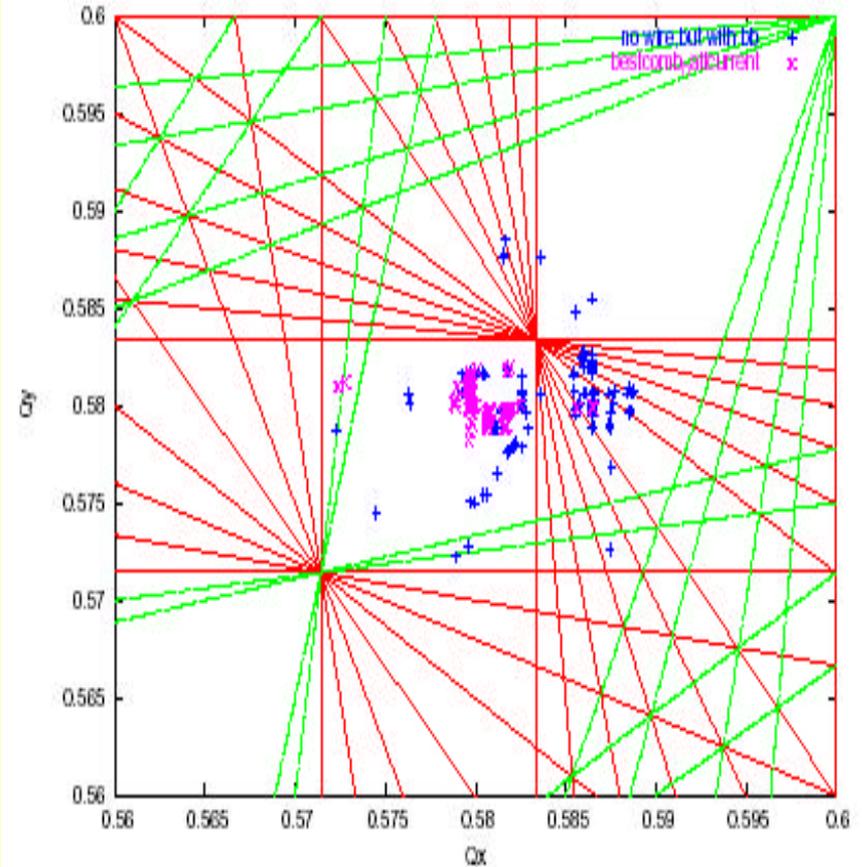
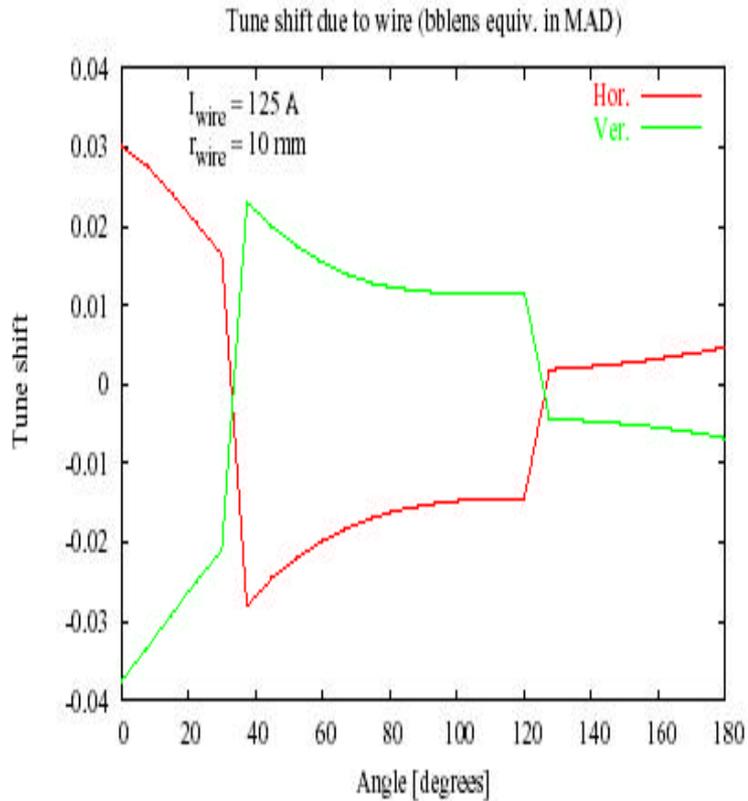
Wire Compensation Strategies

- Proposed for the LHC by J.P. Koutchouk
Compensation in the Tevatron is more complicated.
- Compensation of individual resonances driven by the long-range interactions (analytical)
- Minimizing the norm of the nonlinear map using DA methods (COSY Infinity)
- Lifetime and beam density profiles from tracking with FNAL weak-strong code
- Optics and dynamic aperture using MAD & Sixtrack

Wire locations and helices



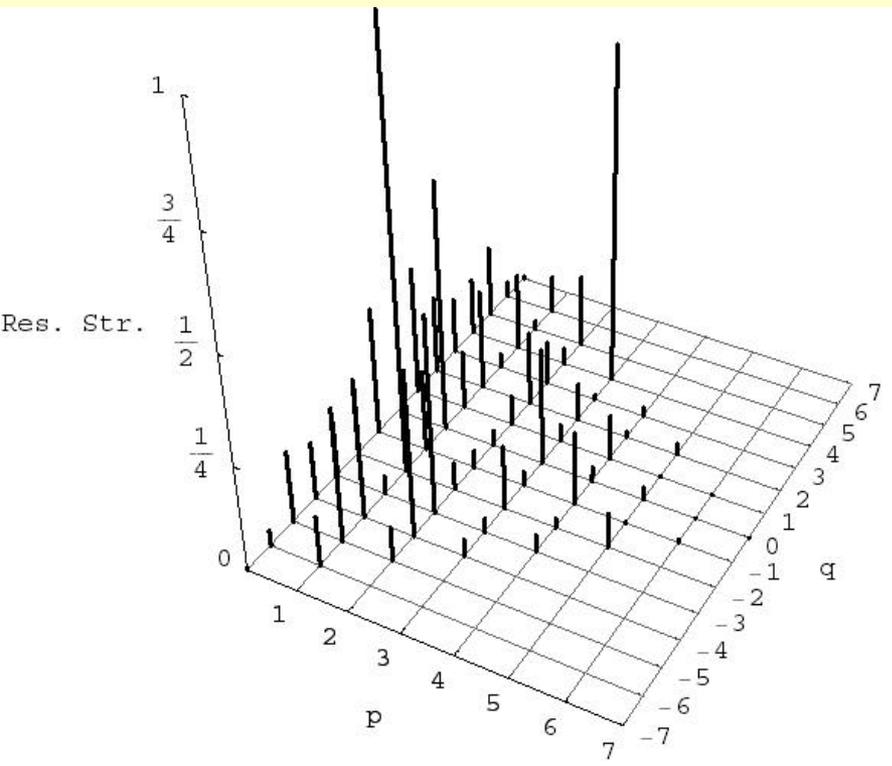
Tunes and Footprints



Tune Shift vs Azimuthal position of wire

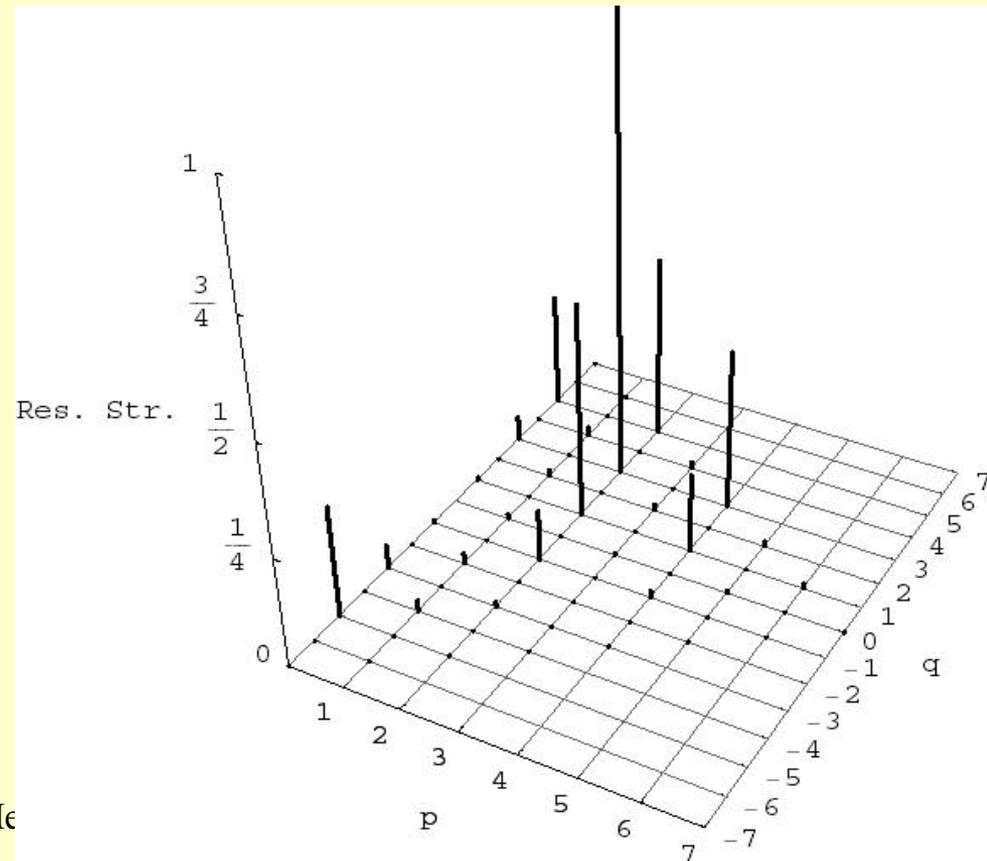
Tune footprint w/wo wire

Resonances vs angle of wire



45 deg

90 deg



Resonance Compensation

Seventh order resonance driving terms in the Hamiltonian

$$U_7 = \text{Re} \sum_p \sum_{m_x, m_y; m_x + m_y = 7} [U_{m_x, m_y, p}^{7, bb} + U_{m_x, m_y, p}^{7, wire}] e^{i(m_x \nu_x + m_y \nu_y - p)\theta} \quad (1)$$

Wire contribution

$$U_{m_x, m_y, p}^{7, wire} = B_W R \sum_{N=6,8,10,\dots} \sum_m C_{N, m; m_x, m_y, p} J_x^{m/2} J_y^{(N+1-m)/2} \quad (2)$$

$$C_{N, m; m_x, m_y, p} = (\dots) \sum_{j_W} (b_N, a_N) \beta_x^{m/2} \beta_y^{(N+1-m)/2} e^{i(m_x \psi_x(\theta) + m_y \psi_y(\theta) + p\theta)} \quad (3)$$

$\sum_{N=6,8,10,\dots}$ includes contributions from main and sub-resonances.

Beam-beam contribution

$$U_{m_x, m_y, p}^{7, bb} = (\dots) \sum_{j, bb} N_p [f \dots] e^{i(m_x \psi_x(\theta) + m_y \psi_y(\theta) + p\theta)} \quad (4)$$

Dependence on the actions (J_x, J_y) is contained in $[f \dots]$ and does not factor out

⇒ Compensation in principle only works at a specific amplitude

Strategy

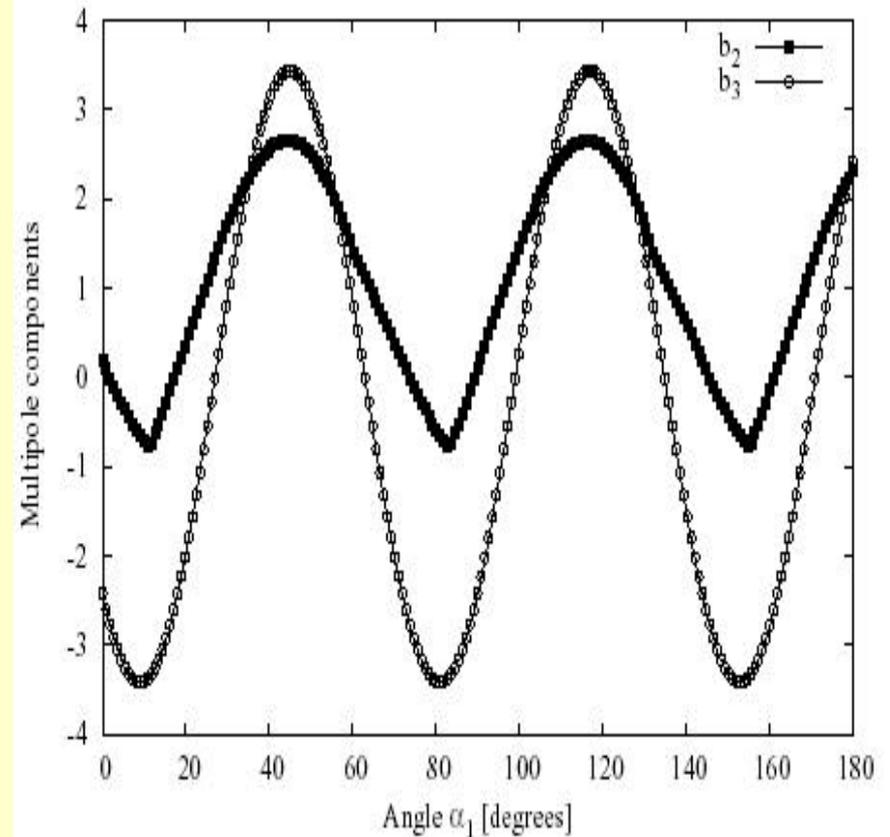
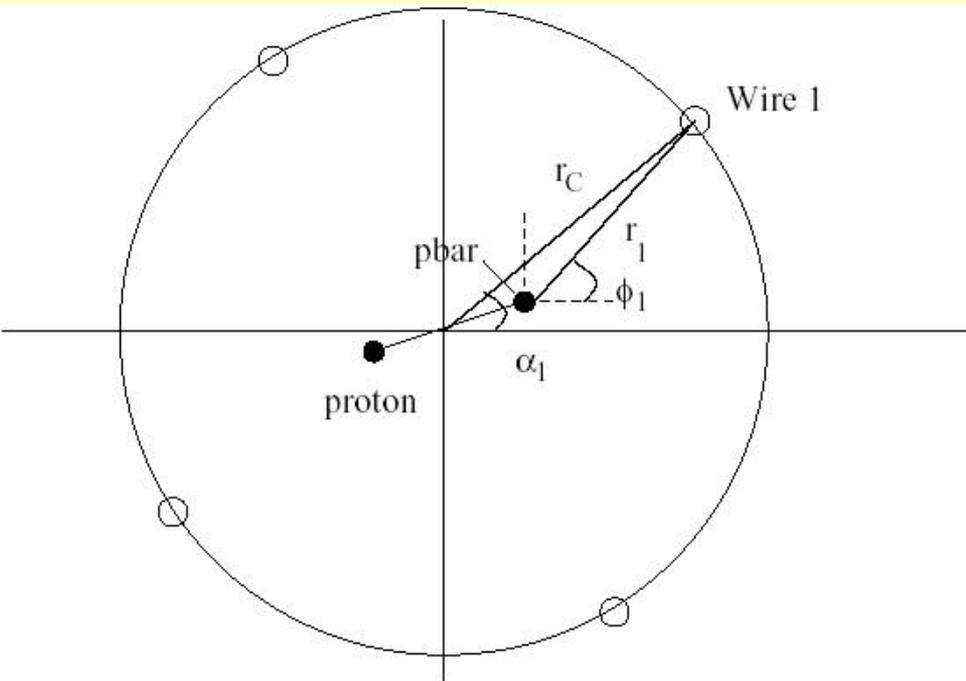
- 1 wire at each location

Compensate the strongest resonances $7\nu_y = p$ and $2\nu_x + 5\nu_y = p$ with $a_0(1), \dots, a_0(4)$ from the 4 wires. If a solution exists, then at a given radius this determines the azimuthal location and hence the $b_0(1), \dots, b_0(4)$.

- Multiple wires at each location

Solutions may exist if none found in Step 1 or other resonances can be compensated.

Multiple wires at one location



Multipole expansions of wires

Field of several infinitely long wires

$$B_y + iB_x = \frac{\mu_0}{2\pi} I_W \sum_{j=1}^{N_W} \sum_{n=0}^{\infty} [-\cos(n+1)\phi_j + i \sin(n+1)\phi_j] \left[\frac{(x+iy)^n}{r_j^{(n+1)}} \right] \quad (1)$$

$$r_j = [(r_C \cos \alpha_j - r_P \cos \theta_P)^2 + (r_C \sin \alpha_j - r_P \sin \theta_P)^2]^{1/2}$$

$$\phi_j = \arctan \left[\frac{(r_C \sin \alpha_j - r_P \sin \theta_P)}{(r_C \cos \alpha_j - r_P \cos \theta_P)} \right] \quad (2)$$

Usual multipole expansion

$$B_y + iB_x = B_0 \sum_{n=0}^{\infty} (b_n + ia_n) \left[\frac{x+iy}{R_{ref}} \right]^n \quad (3)$$

⇒

$$b_n = - \sum_{j=1}^{N_W} \cos(n+1)\phi_j \left[\frac{\langle r_W \rangle}{r_j} \right]^{n+1}, \quad a_n = \sum_{j=1}^{N_W} \sin(n+1)\phi_j \left[\frac{\langle r_W \rangle}{r_j} \right]^{n+1} \quad (4)$$

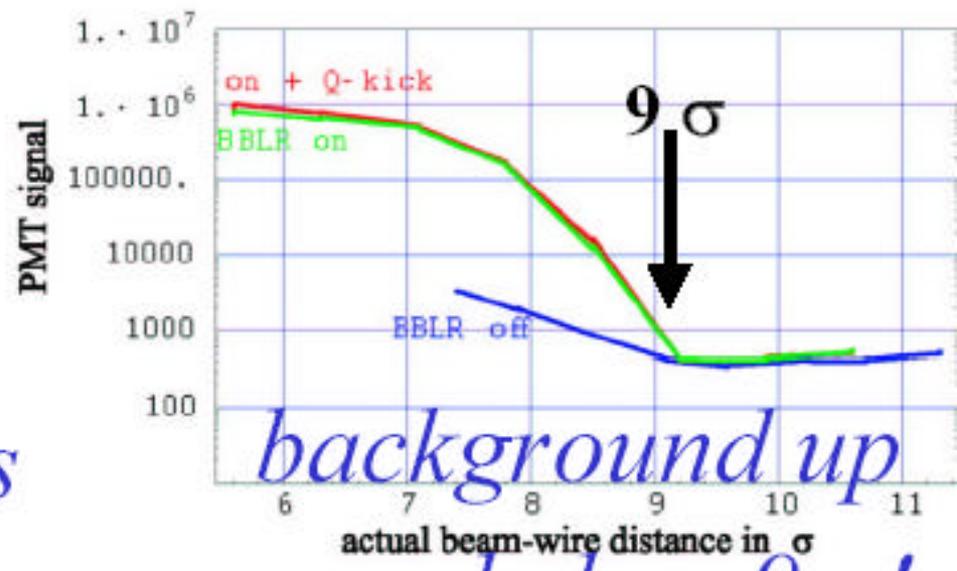
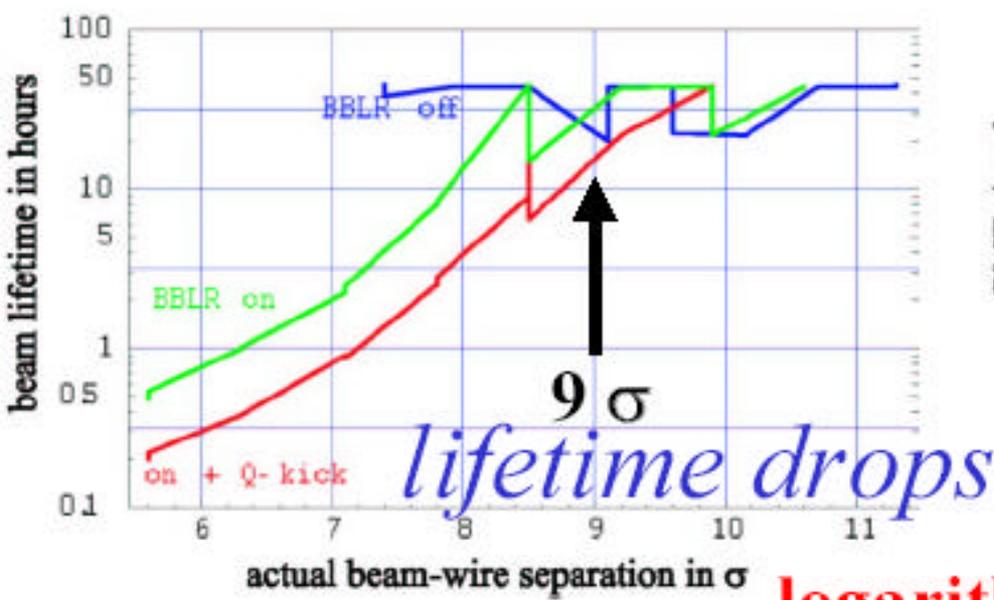
where the main field B_0 and reference radius are

$$B_0 = \frac{\mu_0}{2\pi} \frac{I_W}{\langle r_W \rangle} \quad (5)$$

$$R_{ref} = \langle r_W \rangle = \frac{1}{N_W} \sum_j r_j \quad (6)$$

Each wire creates normal and skew multipoles to all orders.

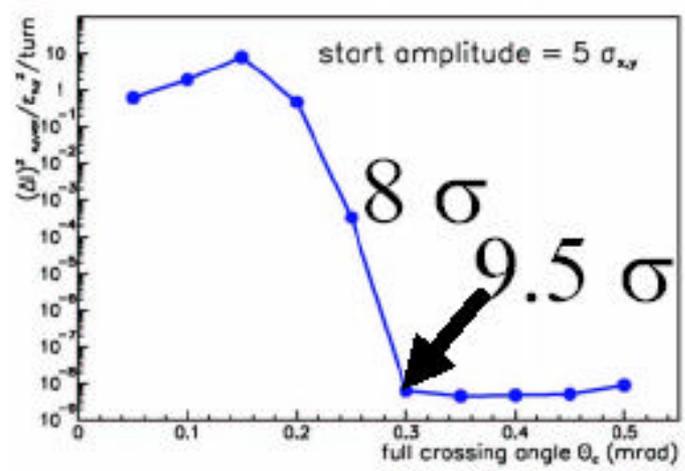
preliminary evidence for diffusion vs. beam-wire distance in SPS



logarithmic scales! *below 9σ!*

F. Zimmermann

compare with LHC simulation:



SPS Wire Parameters

J.P. Koutchouk

Materials	Cu OFHC, Al ₂ O ₃ , stainless steel	m
Active length	2* 0.6	m
Outer/Inner diameters	2.54 (r=1.25σ)/1.54	mm
Intensity	0 to 267	A
Current density	81	A/mm ²
Power	760	W
Water flow	0.36	l/mn
Pressure drop	2.5	bar
Max Pressure	4+2.5=6.5	bar
Pressure of service	60	bar

SPS Wire Design

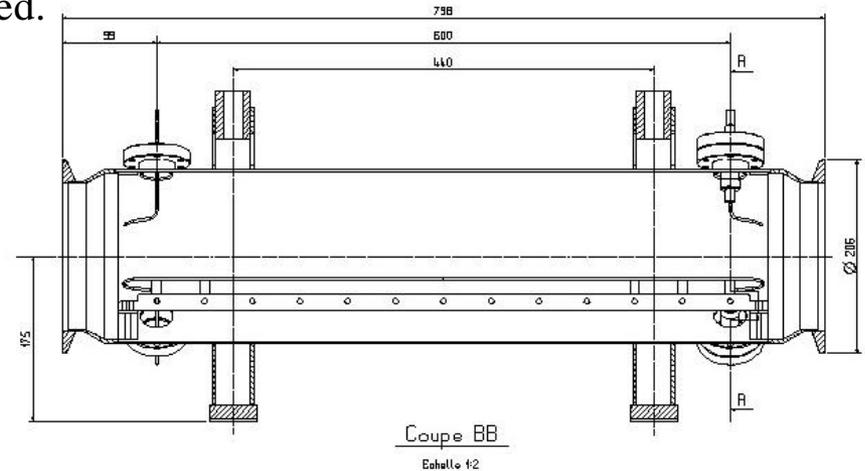
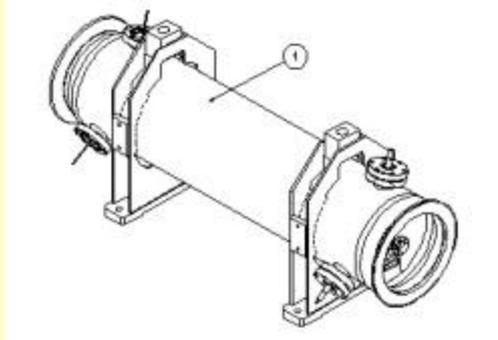
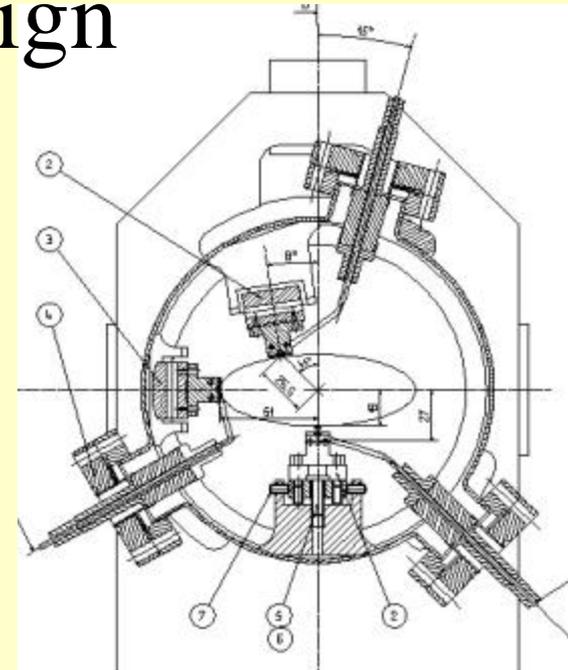
J. Kerby

Recent tests w/ Single Wire in SPS successful

(the proposed 'next step design from CERN shown here)

For further optimization effort is needed on:

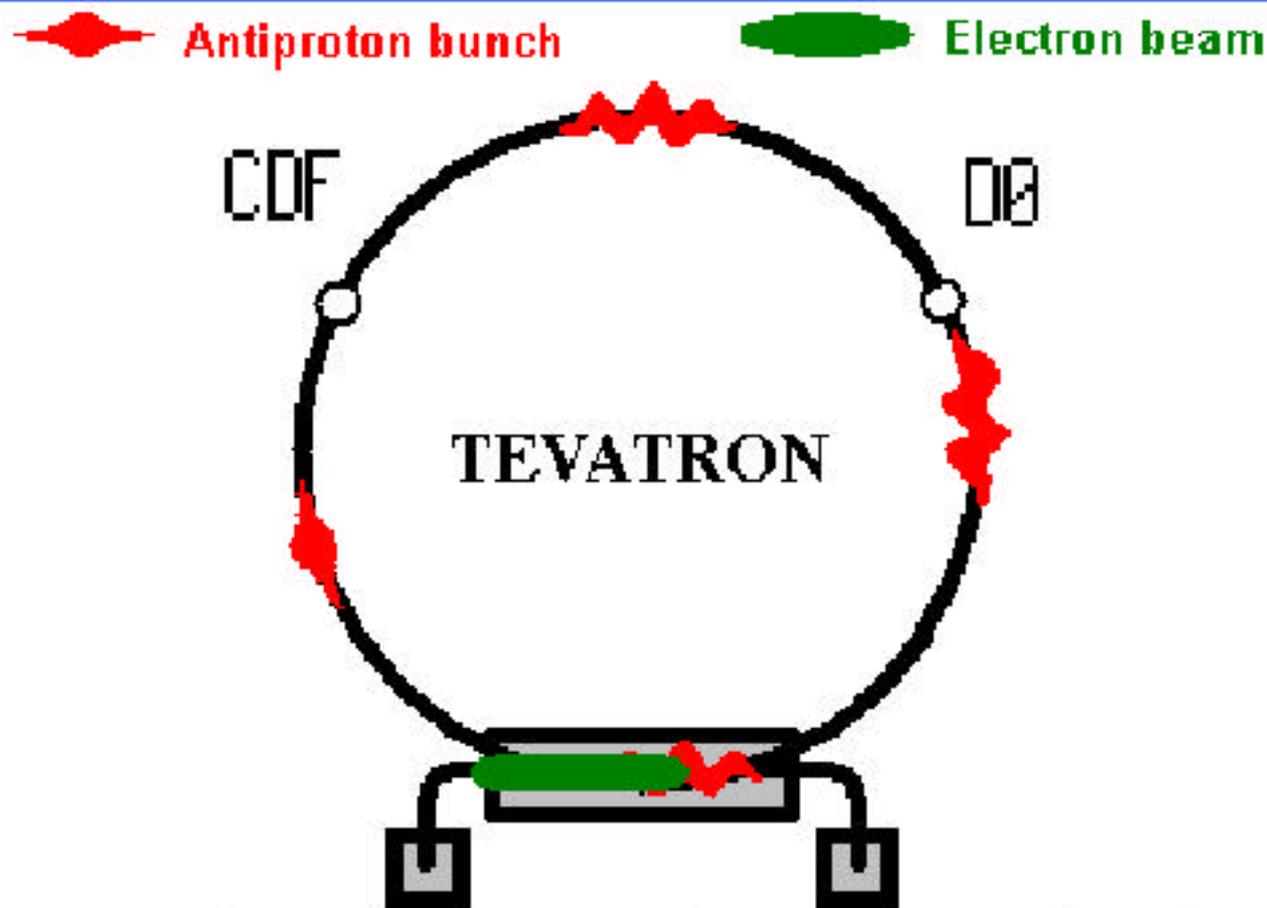
- Mechanical design, overall size, number of wires, and interfaces w/ remainder of machine
- RF / impedance matching
- Possibly cooling, though SPS unit (water cooled) was successful
- Investigation of moveable wire systems, as needed.



Tevatron Wire Summary

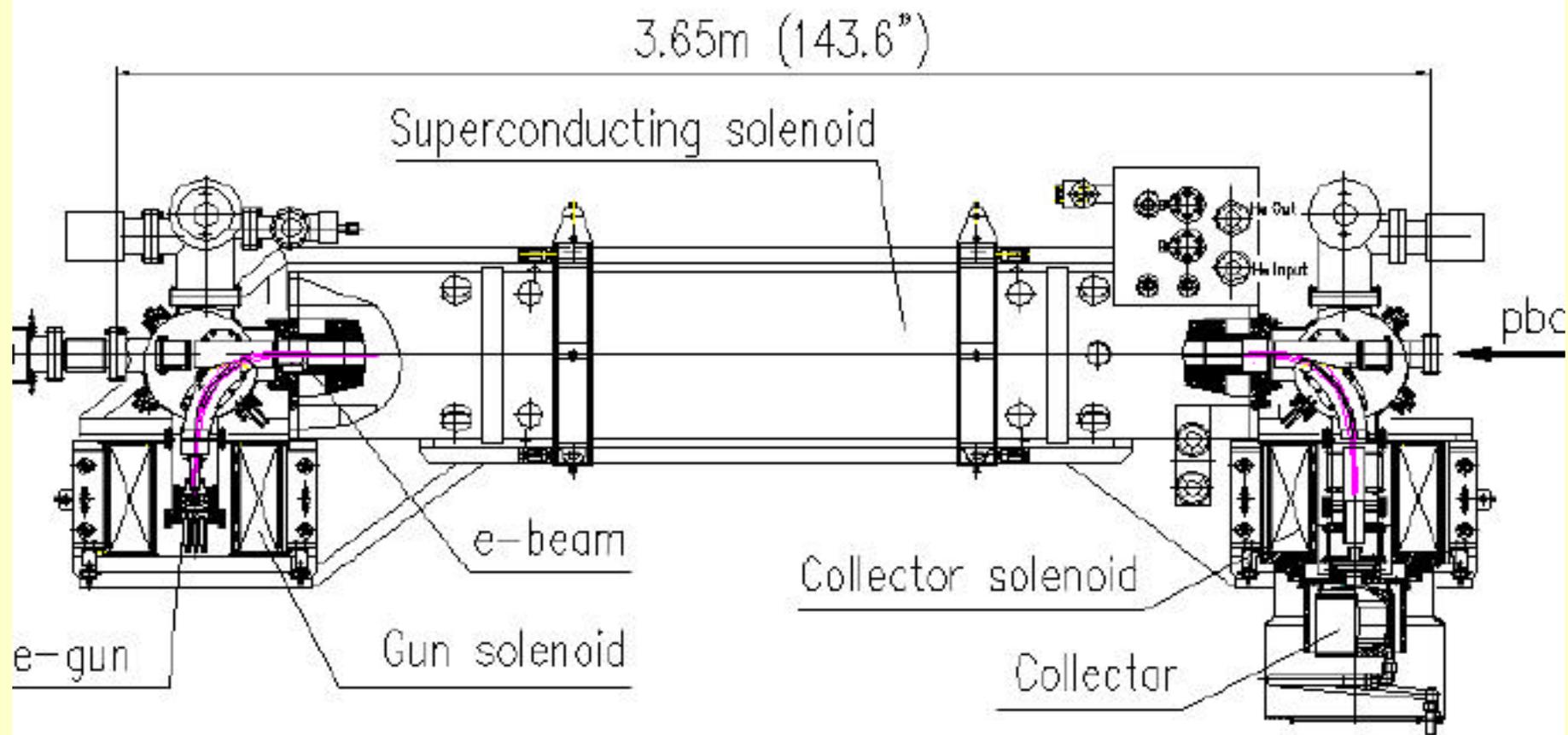
- With 1 wire at each location, tune shifts and resonances depend sensitively on the azimuthal position of wires.
- 1 wire at each location cannot compensate the main 7th order resonances
- Robust compensation and need to adapt to changes in the helix require multiple wires
Exact number to be determined by beam physics and engineering constraints.
- Studies in progress to determine if multi-wire compensation works in principle.

Original Idea Was...



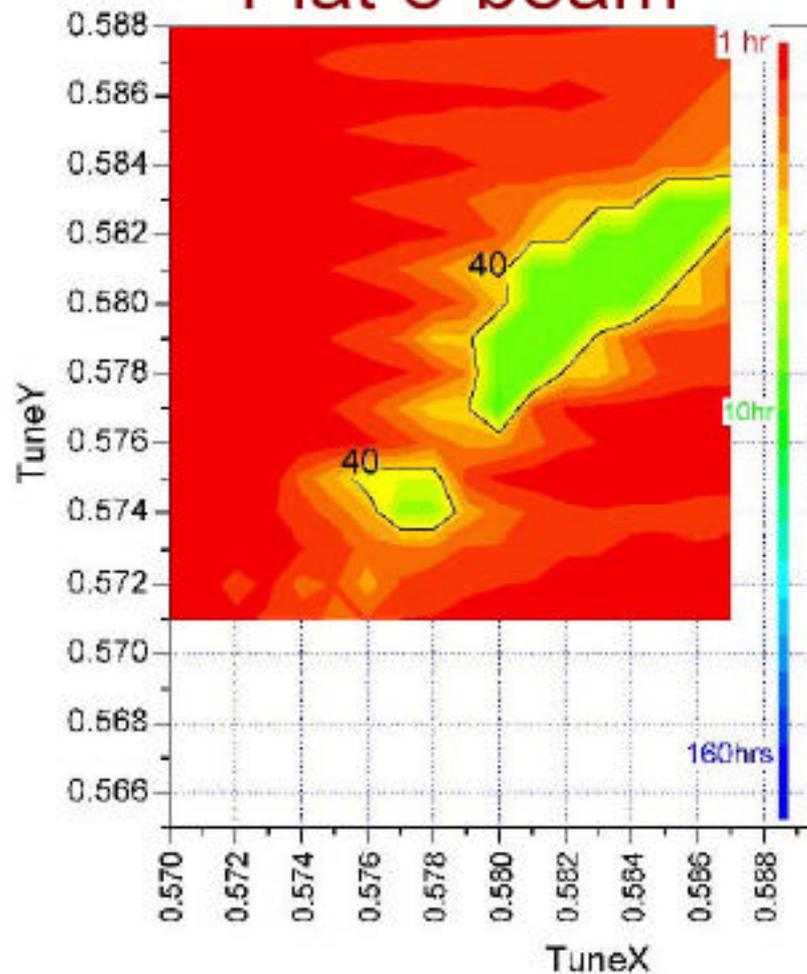
“...to compensate (in average) space charge forces of **positively** charged protons acting on **antiprotons** in the Tevatron by interaction with a **negative charge** of a low energy high-current electron beam “ (1997)

TEL-1: installed Mar.1, 2001

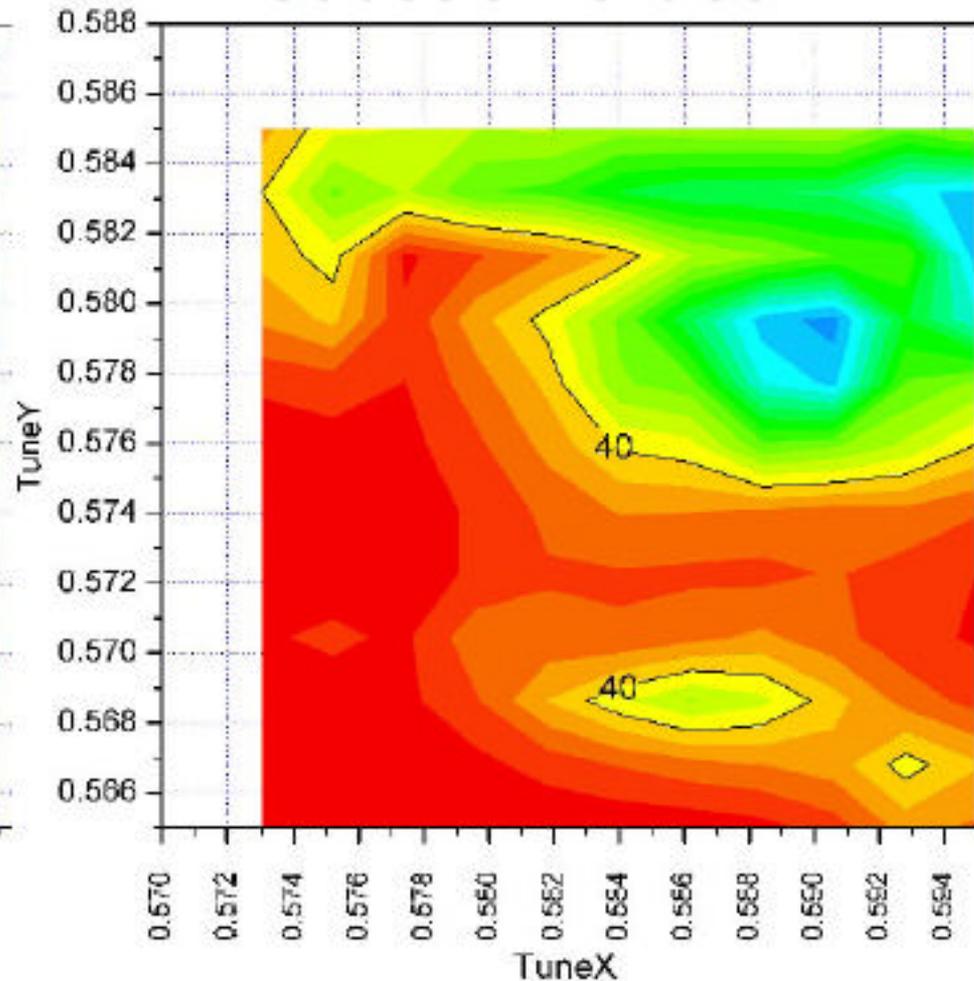


Lifetime vs WP with $dQ_{TEL} \sim 0.004$

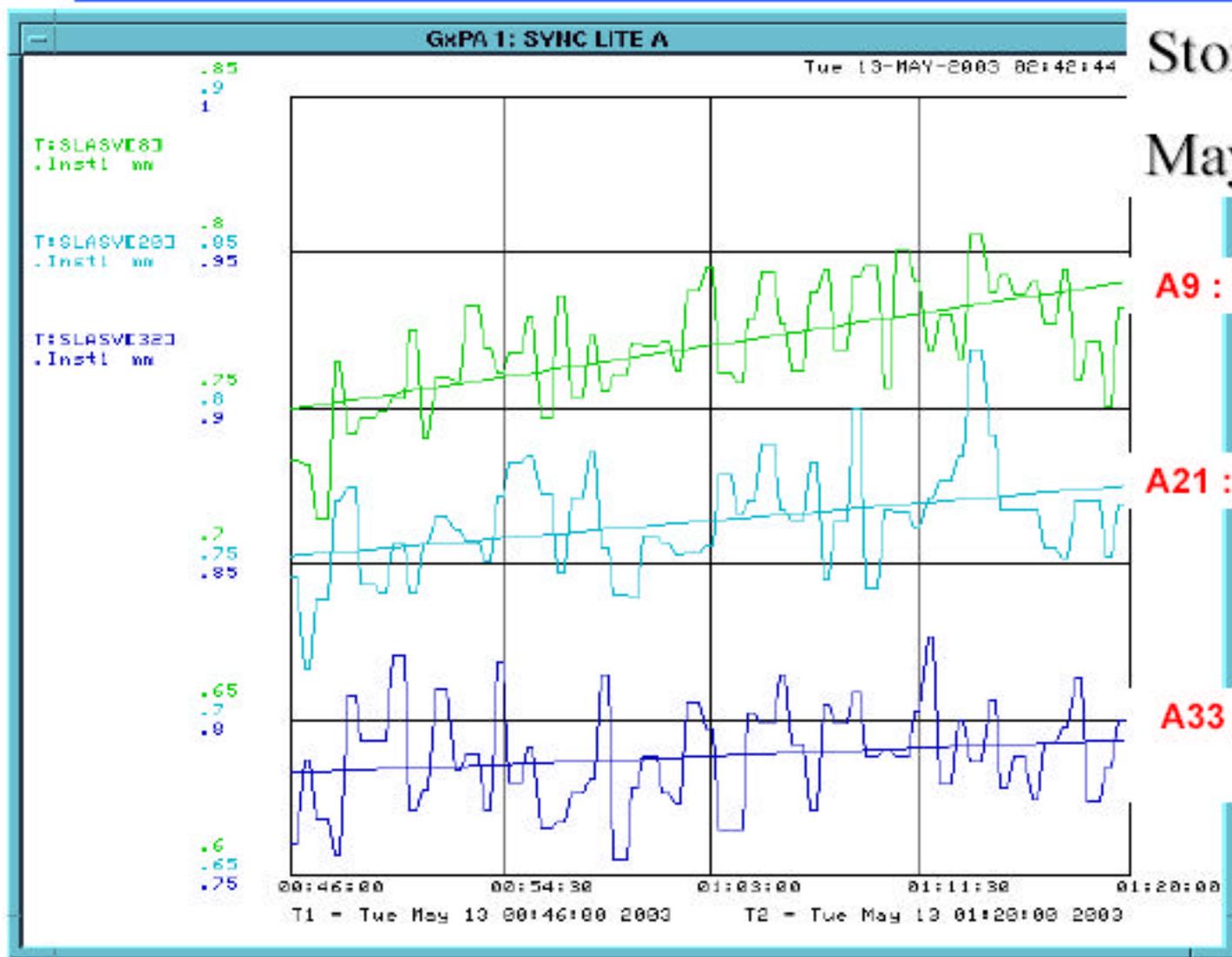
Flat e-beam



Gaussian e-beam



Pbar V-Sizes 34 min after p-pbar collisions initiated



Store #2540

May 12, '03

A9 : 4.1 • •mm mrad/hr

A21 : 2.2 • •mm mrad/hr

A33 : 1 • •mm mrad/hr

-TEL on it

TEL Summary

- **Status:**

- max $dQ \sim 0.009$ tunes shift achieved
- $p(\bar{p})$ lifetime deterioration proved to be due non-linear beam-beam force due to e-beam edges (“soft collimator”)
- after installation of Gaussian e-gun, p -beam lifetime of ~ 160 hrs has been achieved (compare with 40 hrs in stores)
- TEL was used in several stores recently and we’ve got first indications of successful beam-beam compensation : vertical emittance growth rate was reduced for $p\bar{p}$ bunch #33 early in store #2540

- **Work to do:**

- continue to explore BBC at 150, ramp, LB for both $p\bar{p}$ and p
- improve diagnostics (TEL BPM, $P\bar{p}$ Schottky tunemeter, etc)
- wider e-beam
- better beam current and position stabilization
- the second TEL is under construction but the BBC is not the major motivation (\leftarrow spare for the DC beam removal)
- new HV pulser (~ 15 kV instead of 7kV, shorter pulse)