

# Corrections to the

## Christoph Montag's Comment on 90° lattice

parameter	$\mu = 80^\circ$	$\mu = 90^\circ$
$\hat{\beta} = L \cdot \frac{1+\sin(\mu/2)}{\sin \mu}$	$L \cdot 1.668$	$L \cdot 1.707$
$\check{\beta} = L \cdot \frac{1-\sin(\mu/2)}{\sin \mu}$	$L \cdot 0.363$	$L \cdot 0.293$
$\hat{D} = \frac{L^2}{4\rho} \cdot \frac{1+0.5\sin(\mu/2)}{\sin^2(\mu/2)}$	$\frac{L^2}{4\rho} \cdot 3.198$	$\frac{L^2}{4\rho} \cdot 2.707$
$\check{D} = \frac{L^2}{4\rho} \cdot \frac{1-0.5\sin(\mu/2)}{\sin^2(\mu/2)}$	$\frac{L^2}{4\rho} \cdot 1.642$	$\frac{L^2}{4\rho} \cdot 1.293$
$\xi_{\text{nat.}} = -\frac{N}{\pi} \tan(\mu/2)$	$-\frac{N}{\pi} \cdot 0.839$	$-\frac{N}{\pi} \cdot 1.0$

$$\xi_{\text{sext.,}x} = \frac{N}{4\pi} [\hat{m}\hat{D}\hat{\beta} + \check{m}\check{D}\check{\beta}] \quad (1)$$



$$\xi_{\text{sext.,}y} = \frac{-N}{4\pi} [\hat{m}\hat{D}\check{\beta} + \check{m}\check{D}\hat{\beta}] \quad (2)$$



$$\xi_{\text{sext.}} = \xi_{\text{nat.}} \quad (3)$$

$$\xi_{x,y \text{ RHIC}} \approx -52 + \xi_{FODO(6x11)} @ \beta^* = 1m \quad \xi_{FODO(6x11)} \sim -20$$

	parameter	$\mu = 80^\circ$	$\mu = 90^\circ$	$\mu = 80^\circ$	$\mu = 90^\circ$
$\Rightarrow \hat{m} = \frac{\xi_{\text{nat.}}}{\hat{D}(\hat{\beta} + \check{\beta})}$	0.129 · $\frac{4\rho}{L^3}$	0.184 · $\frac{4\rho}{L^3}$	0.254	0.289	
$\check{m} = \hat{m} \cdot \frac{\hat{D}}{\check{D}}$	0.251 · $\frac{4\rho}{L^3}$	0.387 · $\frac{4\rho}{L^3}$	0.495	0.605	

14% H & 22% V

A 90° lattice requires ~~≈ 50%~~ stronger sextupoles than a 80° lattice. Phase advance increase is 12.5%

Dynamic aperture??? ?????

$$\xi_{\text{sext.},x} = \frac{N}{4\pi} \left[ \hat{m} \hat{D} \hat{\beta} + \check{m} \check{D} \check{\beta} \right]$$

$$\xi_{\text{sext.},y} = \frac{-N}{4\pi} \left[ \hat{m} \hat{D} \check{\beta} + \check{m} \check{D} \hat{\beta} \right]$$

$$\xi_{\text{sext.}} = -\xi_{\text{nat.}}$$

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$$\hat{m} = \frac{\xi_{\text{nat.}}}{\hat{D}(\hat{\beta} + \check{\beta})}$$


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$$\check{m} = \hat{m} \cdot \frac{\hat{D}}{\check{D}}$$


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$$\hat{m} = \frac{\xi_{\text{nat.}}}{\hat{D}(\hat{\beta} - \check{\beta})}$$


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$$\check{m} = \hat{m} \cdot \frac{\hat{D}}{\check{D}}$$


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